

$$\begin{aligned}
 1. \quad & \frac{\sqrt{7} - \sqrt{6} + 1}{\sqrt{7} + \sqrt{6} + 1} \xrightarrow{(\sqrt{7} + \sqrt{6})(\sqrt{7} - \sqrt{6})} \\
 & = \frac{(\sqrt{7} - \sqrt{6}) + (\sqrt{7} + \sqrt{6})(\sqrt{7} - \sqrt{6})}{\sqrt{7} + \sqrt{6} + 1} \rightarrow \sqrt{7} - \sqrt{6} \\
 & \quad \text{parantezine alınız.} \\
 & = \frac{(\sqrt{7} - \sqrt{6})(1 + \sqrt{7} + \sqrt{6})}{\sqrt{7} + \sqrt{6} + 1} \\
 & = \sqrt{7} - \sqrt{6}
 \end{aligned}$$

Cevap: D

$$\begin{aligned}
 2. \quad & \sqrt{6} \cdot \sqrt{9} \cdot \sqrt{12} \cdot \dots \cdot \sqrt{75} \rightarrow \frac{75-6}{3} + 1 = 24 \text{ terim} \\
 & = \sqrt{3} \cdot \sqrt{2} \cdot \sqrt{3} \cdot \sqrt{3} \cdot \sqrt{3} \cdot \sqrt{4} \cdot \dots \cdot \sqrt{3} \cdot \sqrt{25} \\
 & = \underbrace{\sqrt{3} \cdot \sqrt{3} \cdot \dots \cdot \sqrt{3}}_{24 \text{ tane}} \cdot \underbrace{\sqrt{2} \cdot \sqrt{3} \cdot \sqrt{4} \cdot \dots \cdot \sqrt{25}}_A \\
 & = (\sqrt{3})^{24} \cdot A \\
 & = 3^{12} \cdot A
 \end{aligned}$$

Cevap: D

$$\begin{aligned}
 3. \quad & 82 = a \text{ dersek} \\
 & \sqrt{82 \cdot 84 + 1} = \sqrt{a \cdot (a+2) + 1} = \sqrt{a^2 + 2a + 1} \\
 & = \sqrt{(a+1)^2} \\
 & = a + 1 \\
 & = 82 + 1 \\
 & = 83
 \end{aligned}$$

Cevap: E

$$\begin{aligned}
 4. \quad & \frac{\sqrt{7} - 1}{1 + \sqrt{2}} = M \\
 x \quad & \frac{\sqrt{7} + 1}{1 - \sqrt{2}} = x \\
 & \frac{(\sqrt{7} - 1)(\sqrt{7} + 1)}{(1 + \sqrt{2})(1 - \sqrt{2})} = M \cdot x \\
 & \frac{7 - 1}{1 - 2} = M \cdot x \\
 & -6 = M \cdot x \\
 & x = -\frac{6}{M}
 \end{aligned}$$

Cevap: E

$$\begin{aligned}
 5. \quad & a = 343 \\
 & b = 370 \\
 & \sqrt{344 \cdot 370 - 343 \cdot (371)} = \sqrt{(a+1) \cdot b - a \cdot (b+1)} \\
 & = \sqrt{ab + b - ab - a} \\
 & = \sqrt{b - a} \\
 & = \sqrt{370 - 343} \\
 & = \sqrt{27} \\
 & = 3\sqrt{3}
 \end{aligned}$$

Cevap: E

$$\begin{aligned}
 6. \quad & a = 23 \Rightarrow \sqrt{1 + 22 \cdot \sqrt{1 + (a+2) \cdot a}} \\
 & = \sqrt{1 + 22 \cdot \sqrt{a^2 + 2a + 1}} \\
 & = \sqrt{1 + 22 \cdot (a+1)} \\
 & b = 22 \Rightarrow \sqrt{1 + 22 \cdot 24} \\
 & = \sqrt{1 + b \cdot (b+2)} \\
 & = \sqrt{b^2 + 2b + 1} \\
 & = b + 1 \\
 & = 22 + 1 \\
 & = 23
 \end{aligned}$$

Cevap: D

$$7. \quad \sqrt[4]{\frac{a}{b}} = 3 \Rightarrow \frac{a}{b} = 3^4$$

$$\left(\frac{6}{a}\right)^2 = 4 \Rightarrow \frac{6}{a} = 2$$

$$\Rightarrow a = 3$$

$$\frac{3}{b} = 81 \Rightarrow b = \frac{1}{27}$$

$$a.b = 3 \cdot \frac{1}{27} = \frac{1}{9} = \frac{1}{3^2}$$

Cevap: B

$$8. \quad \frac{\sqrt{2}+1}{\sqrt{6}+\sqrt{3}-2-\sqrt{2}} = \frac{\sqrt{2}+1}{\sqrt{3}(\sqrt{2}+1)-\sqrt{2}(\sqrt{2}+1)}$$

$$= \frac{\sqrt{2}+1}{(\sqrt{2}+1)(\sqrt{3}-\sqrt{2})}$$

$$= \frac{1}{\sqrt{3}-\sqrt{2}} \cdot \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}+\sqrt{2}}$$

$$= \frac{\sqrt{3}+\sqrt{2}}{3-2} = \sqrt{3}+\sqrt{2}$$

Cevap: B

$$9. \quad \frac{2}{\sqrt{6-2\sqrt{5}}} - \frac{2}{\sqrt{6+2\sqrt{5}}}$$

$$= \frac{2}{\sqrt{5-1}} - \frac{2}{\sqrt{5+1}}$$

$$= \frac{2(\sqrt{5}+1) - 2(\sqrt{5}-1)}{4}$$

$$= \frac{2\sqrt{5}+2-2\sqrt{5}+2}{4} = \frac{4}{4} = 1$$

Cevap: B

$$10. \quad (\sqrt{3}-\sqrt{2})^3 \cdot (\sqrt{3}+\sqrt{2})^4$$

$$(\sqrt{3}-\sqrt{2})^3 \cdot (\sqrt{3}+\sqrt{2})^3 \cdot (\sqrt{3}+\sqrt{2})$$

$$((\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2}))^3 \cdot (\sqrt{3}+\sqrt{2})$$

$$(3-2)^3 \cdot (\sqrt{3}+\sqrt{2})$$

$$1^3 \cdot (\sqrt{3}+\sqrt{2})$$

$$\sqrt{3}+\sqrt{2}$$

Cevap: B

$$11. \quad \sqrt{\frac{\sqrt{80}+4}{\sqrt{6}-\sqrt{20}}} = \sqrt{\frac{4\sqrt{5}+4}{\sqrt{6}-2\sqrt{5}}}$$

$$= \sqrt{\frac{4(\sqrt{5}+1)}{\sqrt{5}-1}} = \sqrt{\frac{4 \cdot (\sqrt{5}+1)^2}{5-1}} = \sqrt{(\sqrt{5}+1)^2}$$

$$= \sqrt{5}+1$$

Cevap: D

$$12. \quad (\sqrt{3}-\sqrt{2})^{22} \cdot (5+2\sqrt{6})^{11} - \sqrt{6}$$

$$((\sqrt{3}-\sqrt{2})^2)^{11} \cdot (5+2\sqrt{6})^{11} - \sqrt{6}$$

$$(3+2-2\sqrt{6})^{11} \cdot (5+2\sqrt{6})^{11} - \sqrt{6}$$

$$(5-2\sqrt{6})^{11} (5+2\sqrt{6})^{11} - \sqrt{6}$$

$$((5-2\sqrt{6})(5+2\sqrt{6}))^{11} - \sqrt{6}$$

$$(25-24)^{11} - \sqrt{6}$$

$$1^{11} - \sqrt{6}$$

$$1 - \sqrt{6}$$

Cevap: C

$$13. \quad \sqrt{3-\sqrt{1+2\sqrt{12}}} \cdot \sqrt{3+\sqrt{1+2\sqrt{12}}}$$

$$\sqrt{(3-\sqrt{1+2\sqrt{12}})(3+\sqrt{1+2\sqrt{12}})}$$

$$\sqrt{9-(1+2\sqrt{12})}$$

$$\sqrt{8-2\sqrt{12}}$$

$$= \sqrt{6}-\sqrt{2}$$

Cevap: C

$$14. \quad \sqrt{39^2-9^2-12^2}$$

$$= \sqrt{3^2(13^2-3^2-4^2)}$$

$$= \sqrt{3^2 \cdot (169-9-16)}$$

$$= \sqrt{3^2 \cdot 144}$$

$$= \sqrt{3^2 \cdot 12^2}$$

$$= 3 \cdot 12$$

$$= 36$$

Cevap: A