

$$\begin{aligned}
1. \quad & \log(x-5) + \log(x+4) = 1 \\
& \log(x-5)(x+4) = 1 \\
& (x-5)(x+4) = 10 \\
& x^2 + 4x - 5x - 20 = 10 \\
& x^2 - x - 30 = 0 \\
& (x-6)(x+5) = 0 \\
& x-6 = 0 \rightarrow x = 6 \\
& x+5 = 0 \rightarrow x = -5 \\
\Rightarrow & \Sigma x = 6 - 5 = 1
\end{aligned}$$

Cevap: C

$$\begin{aligned}
2. \quad & \log_x(1 + \log_x 8) = 2 \\
& x^2 = 1 + \log_x 8 \\
x = 2 & \quad \text{için ;} \quad 2^2 = 1 + \log_2 8 \\
& 4 = 4 + \log_2 2^3 \\
& 4 = 1 + 3 \cdot \log_2 2 \\
& 4 = 4
\end{aligned}$$

Cevap: C

$$\begin{aligned}
3. \quad & \log 5 = \frac{\log_3 5}{\log_3 10} = \frac{\log_3 5}{\log_3 2 + \log_3 5} = \frac{x}{1} \\
& \left. \begin{aligned} \log_3 5 &= x \cdot k \\ \log_3 2 + \log_3 5 &= k \\ \log_3 2 + x \cdot k &= k \\ \log_3 2 &= k - x \cdot k \end{aligned} \right\} \begin{aligned} \frac{\log_3 10}{\log_3 2} &= \frac{\log_3 2 + \log_3 5}{\log_3 2} \\ &= \frac{k - x \cdot k + x \cdot k}{k - xk} \\ &= \frac{k}{k(1-x)} = \frac{1}{1-x} \end{aligned}
\end{aligned}$$

Cevap: B

$$\begin{aligned}
4. \quad & 3^{3x} = 10 \\
& \log_3 10 = 3x \\
& \frac{1}{3} \log_3 10 = x \Rightarrow \log_3 10^{\frac{1}{3}} = x
\end{aligned}$$

Cevap: D

$$\begin{aligned}
5. \quad & \frac{1}{1 + \log_{\frac{1}{5}} 15} = \frac{1}{\log_{\frac{1}{5}} \frac{1}{5} + \log_{\frac{1}{5}} 15} \\
& = \frac{1}{\log_{\frac{1}{5}} \frac{1}{5} \cdot 15} = \frac{1}{\log_{\frac{1}{5}} 3} \\
& = \frac{1}{\log_5 - 1^3} = \frac{1}{-\log_5 3} = -\log_3 5
\end{aligned}$$

Cevap: C

$$\begin{aligned}
6. \quad & \frac{\frac{1}{2} \log_{2^2} 3^{\frac{1}{2}}}{2 \log_2 3^2} = \frac{\frac{1}{2} \cdot \log_2 3}{2 \cdot \frac{2}{2} \cdot \log_2 3} = \frac{\frac{1}{2}}{2} = \frac{1}{4}
\end{aligned}$$

Cevap: D

$$\begin{aligned}
7. \quad & \log 2 = m \\
& \log 3 = n \\
& \log(1, 2) = \log \frac{12}{10} = \log 12 - \log 10 \\
& = \log 3 + \log 4 - 1 \\
& = \log 3 + \log 2^2 - 1 \\
& = \log 3 + 2 \log 2 - 1 \\
& = n + 2 \cdot m - 1
\end{aligned}$$

Cevap: B

$$\begin{aligned}
8. \quad & 5 \cdot \log x = \log 9 + \frac{1}{2} \log 3 \\
& = \log 9 + \log \sqrt{3} \\
5 \log x &= \log 9 \cdot \sqrt{3} \\
\log x^5 &= \log 9 \cdot \sqrt{3} \\
x^5 &= 3^2 \cdot 3^{\frac{1}{2}} \\
x^5 &= 3^{\frac{5}{2}} \Rightarrow x = 3^{\frac{1}{2}} = \sqrt{3}
\end{aligned}$$

Cevap: A

$$9. \left. \begin{array}{l} \log_5 m = a \\ \log_m 2 = b \end{array} \right\} \log_5 m \cdot \log_m 2 = a \cdot b$$

$$\log_5 2 = a \cdot b$$

$$\log_{\sqrt{5}} 8 = \log_5 \frac{1}{2} 2^3 = \frac{3}{\frac{1}{2}} \log_5 2$$

$$= 6 \cdot \log_5 2 = 6 \cdot a \cdot b$$

Cevap: E

$$10. \log_4 2 + \log_9 3 - \log_3 27$$

$$\log_{2^2} 2 + \log_{3^2} 3 - \log_3 3^3$$

$$\frac{1}{2} + \frac{1}{2} - 3 = 1 - 3 = -2$$

Cevap: B

$$11. \log_{\sqrt{125}} \frac{1}{64} = \log_5 \frac{3^{2-6}}{2} = \frac{-6}{\frac{3}{2}} \log_5 2 = -4 \cdot \log_5 2$$

$$= -4 \cdot x$$

Cevap: E

$$12. A) \log_4 16 = \log_4 4^2 = 2 \cdot \log_4 4 = 2$$

A şıkkı yanlıştır.

Cevap: A

$$13. \alpha = \log 2$$

$$\beta = \log 50$$

$$\beta = \log 50 = \log \frac{100}{2} = \log 100 - \log 2$$

$$= \log 10^2 - \log 2$$

$$= 2 - \alpha$$

$$\beta = 2 - \alpha$$

Cevap: A

$$14. \log_2 \frac{3x-2}{x+1} = 1$$

$$\frac{3x-2}{x+1} = 2$$

$$3x-2 = 2x+2$$

$$x = 4$$

Cevap: B

$$15. \log_2 [\log_2 2(\ln(x+1))] = 1$$

$$2 = \log_2 2(\ln(x+1))$$

$$4 = 2 \ln(x+1)$$

$$2 = \ln(x+1)$$

$$e^2 = x+1$$

$$x = e^2 - 1$$

Cevap: A

$$16. \log_x 4 + \log_x 6 + \log_x 9 = 27 \log_8 2$$

$$\log_x 4 \cdot 6 \cdot 9 = 27 \log_2 3^2$$

$$\log_x 4 \cdot 6 \cdot 9 = 27 \cdot \frac{1}{3}$$

$$\log_x 4 \cdot 6 \cdot 9 = 3$$

$$x^3 = 4 \cdot 6 \cdot 9 = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3$$

$$x = 2 \cdot 3 = 6$$

Cevap: E

$$17. \frac{2}{\log_3 36} + \frac{1}{\log_4 36} = 2 \cdot \log_{36} 3 + \log_{36} 4$$

$$= \log_{36} 9 + \log_{36} 4$$

$$= \log_{36} 36 = 1$$

Cevap: B

$$18. \log_9 2 = \log_3 2^2 = \frac{1}{2} \log_3 2 = a$$

$$\log_3 2 = 2a$$

$$\begin{aligned} \log_6 16 &= \frac{\log_3 16}{\log_3 6} = \frac{\log_3 2^4}{\log_3 2 + \log_3 3} \\ &= \frac{4 \cdot 2a}{2a + 1} = \frac{8a}{2a + 1} \end{aligned}$$

Cevap: A

$$\begin{aligned} 19. \frac{\log_4 64}{\log_3 81} + \frac{\log_5 125}{\log_2 16} \\ &= \frac{\log_4 4^3}{\log_3 3^4} + \frac{\log_5 5^3}{\log_2 2^4} = \frac{3}{4} + \frac{3}{4} \\ &= \frac{6}{4} = \frac{3}{2} \end{aligned}$$

Cevap: D

$$\begin{aligned} 20. \log_4 (64 \log_x 81) &= 4 \\ 4^4 &= 64 \cdot \log_x 81 \\ 2^8 &= 2^6 \cdot \log_x 81 \\ 2^2 &= \log_x 81 \\ x^4 &= 81 \Rightarrow x = 3 \end{aligned}$$

Cevap: D